nag_ode_ivp_adams_interp (d02qzc)

1. Purpose

nag_ode_ivp_adams_interp (d02qzc) interpolates components of the solution of a non-stiff system of first order ordinary differential equations from information provided by nag_ode_ivp_adams_roots (d02qfc). Normally this function will be used in conjunction with the integration function, nag_ode_ivp_adams_roots (d02qfc), operating in one-step mode.

2. Specification

3. Description

nag_ode_ivp_adams_interp evaluates the first **nwant** components of the solution of a non-stiff system of first order ordinary differential equations at any point using the method of Watts and Shampine (1986) and information generated by nag_ode_ivp_adams_roots (d02qfc). nag_ode_ivp_adams_interp should not normally be used to extrapolate outside the current range of the values produced by the integration routine.

4. Parameters

negf

Input: the number of differential equations. Constraint: $\mathbf{neqf} \geq 1$.

twant

Input: the point at which components of the solution and derivative are to be evaluated. **twant** should not normally be an extrapolation point, that is **twant** should satisfy

```
opt.tcurr-opt.hlast \leq twant \leq opt.tcurr.
```

or if integration is proceeding in the negative direction

```
opt.tcurr - opt.hlast \ge twant \ge opt.tcurr.
```

Extrapolation is permitted but not recommended and a **fail.code** value of **NW_EXTRAPOLATION** is returned whenever extrapolation is attempted.

nwant

Input: the number of components of the solution and derivative whose values, at **twant**, are required. The first **nwant** components are evaluated.

```
Constraint: 1 \leq \text{nwant} \leq \text{neqf}.
```

ywant[nwant]

Output: $\mathbf{ywant}[i-1]$ contains the calculated value of the *i*th component of the solution at \mathbf{twant} , for $i=1,2,\ldots,\mathbf{nwant}$.

ypwant[nwant]

Output: $\mathbf{ypwant}[i-1]$ contains the calculated value of the *i*th component of the derivative at \mathbf{twant} , for $i=1,2,\ldots,\mathbf{nwant}$.

opt

Input: the structure of type Nag_ODE_Adams as output from the integration function nag_ode_ivp_adams_roots (d02qfc). The structure ${\bf must}$ be passed unchanged. (See Section 6 for comments about deallocation of memory from ${\bf opt}$.)

fail

The NAG error parameter, see the Essential Introduction to the NAG C Library. It is recommended that **fail.print** be set to **TRUE**.

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5. Error Indications and Warnings

NE_NO_INTEGRATE

The integrator function nag_ode_ivp_adams_roots (d02qfc) has not been called.

NE_NEQF

The value of **neqf** supplied is not the same as that given to the setup function nag_ode_ivp_adams_setup (d02qwc). **neqf** = $\langle value \rangle$ but the value given to nag_ode_ivp_adams_setup (d02qwc) was $\langle value \rangle$.

NE_NWANT_GT

nwant is greater than the value of **neqf** given to the setup function nag_ode_ivp_adams_setup (d02qwc). **nwant** = $\langle value \rangle$, **neqf** = $\langle value \rangle$.

NE_INT_ARG_LT

On entry, **nwant** must not be less than 1: **nwant** = $\langle value \rangle$.

NE_NO_STEPS

No successful integration steps were taken in the call(s) to the integration function nag_ode_ivp_adams_roots (d02qfc).

NW_EXTRAPOLATION

Extrapolation requested, **twant** = $\langle value \rangle$.

6. Further Comments

When interpolation for only a few components is required then it is more efficient to order the components of interest so that they are numbered first.

The structure **opt** will contain pointers which have been allocated memory during a call to nag_ode_ivp_adams_setup (d02qwc). This allocated memory is used by nag_ode_ivp_adams_roots (d02qfc) and nag_ode_ivp_adams_interp. When all calls to these functions have been completed the function nag_ode_ivp_adams_free (d02qyc) may be called to free the allocated memory from the structure.

6.1. Accuracy

The error in interpolation is of a similar order to the error arising from the integration. The same order of accuracy can be expected when extrapolating using nag_ode_ivp_adams_interp. However, the actual error in extrapolation will, in general, be much larger than for interpolation.

6.2. References

Watts H A and Shampine L F (1986) Smoother Interpolants for Adams Codes SIAM J. Sci. Statist. Comput. 7 334–345.

7. See Also

nag_ode_ivp_adams_roots (d02qfc) nag_ode_ivp_adams_setup (d02qwc) nag_ode_ivp_adams_free (d02qyc)

8. Example

We solve the equation

$$y'' = -y,$$
 $y(0) = 0, y'(0) = 1$

reposed as

$$\begin{array}{ccc} y_1' & = & y_2 \\ y_2' & = & -y_1 \end{array}$$

over the range $[0, \pi/2]$ with initial conditions $y_1 = 0$ and $y_2 = 1$ using vector error control (vectol = TRUE) and nag_ode_ivp_adams_roots (d02qfc) in one-step mode (one_step = TRUE). nag_ode_ivp_adams_interp is used to provide solution values at intervals of $\pi/16$.

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8.1. Program Text

```
/* nag_ode_ivp_adams_interp(d02qzc) Example Program
 * Copyright 1991 Numerical Algorithms Group.
 * Mark 2, 1991.
 * Mark 6 revised, 2000.
 */
#include <nag.h>
#include <stdio.h>
#include <nag_stdlib.h>
#include <nagd02.h>
#include <nagx01.h>
static void ftry03(Integer neqf, double x, double y[], double yp[],
                    Nag_User *comm);
#define NEQF 2
#define TSTART 0.0
main()
  double atol[NEQF], rtol[NEQF], y[NEQF], ywant[NEQF];
  Boolean crit, alter_g, vectol, one_step, sophist; double t, tinc, tout, tcrit, twant, hmax, pi;
  Integer max_step, i, j, neqf, neqg, nwant;
  Nag_Start state;
  Nag_ODE_Adams opt;
  static NagError fail;
  fail.print = TRUE;
  Vprintf("d02qzc Example Program Results\n");
  pi = X01AAC;
  state = Nag_NewStart;
  neqf = NEQF;
  neqg = 0;
  sophist = FALSE;
  vectol = TRUE;
  for (i = 0; i < 2; ++i)
      atol[i] = 1e-08;
      rtol[i] = 0.0001;
  one_step = TRUE;
  crit = TRUE;
  tinc = pi * 0.0625;
  tcrit = tinc * 8.0;
  tout = tcrit;
  max_step = 500;
hmax = 2.0;
  t = TSTART;
  twant = TSTART + tinc;
  nwant = 2;
  y[0] = 0.0;
  y[1] = 1.0;
  Vprintf("\n
                 Τ
                          Y(1)
                                   Y(2)\n");
  Vprintf(" %6.4f
                     \%7.4f \%7.4f \n",t, y[0], y[1]);
  d02qwc(&state, neqf, vectol, atol, rtol, one_step, crit,
         tcrit, hmax, max_step, neqg, &alter_g, sophist, &opt, &fail);
  j = 1;
  while (t < tout && fail.code == NE_NOERROR)</pre>
      d02qfc(neqf, ftry03, &t, y, tout, NULLDFN, NAGUSER_DEFAULT, &opt, &fail);
```

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8.2. Program Data

None.

8.3. Program Results

d02qzc Example Program Results

```
Τ
            Y(1)
                     Y(2)
0.0000
           0.0000 1.0000
         0.1951 0.9808
0.3827 0.9239
0.5556 0.8315
0.1963
0.3927
0.5890
0.7854
           0.7071 0.7071
0.9817
          0.8315 0.5556
          0.9239 0.3827
0.9808 0.1951
1.1781
1.3744
         1.0000 0.0000
1.5708
```

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